

MINLP – Global Solvers

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October 8th, 2015, CO@Work, Berlin



ANTIGONE (Algorithms for coNTinuous / Integer Global Optimization of Nonlinear Equations)

- ▶ by R. Misener (Imperial) and C.A. Floudas (Princeton)
- ▶ originating from a solver for pooling problems
- ▶ available as commercial solver in GAMS
- ▶ Misener and Floudas [2012a,b, 2014], Misener [2012]



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BARON (Branch And Reduce Optimization Navigator)

- ▶ by N. Sahinidis (CMU) and M. Tawarmalani (Purdue)
- ▶ one of the first general purpose codes
- ▶ available as commercial solver in AIMMS, AMPL, GAMS
- ▶ Tawarmalani and Sahinidis [2002, 2004, 2005]



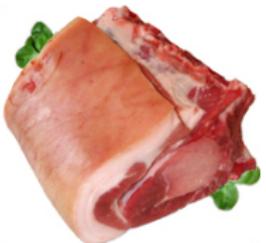
Couenne (Convex Over and Under ENvelopes for Nonlinear Estimation)

- ▶ by P. Belotti (CMU, Clemson, now FICO)
- ▶ COIN-OR open source solver based on Bonmin (based on CBC and Ipopt)
- ▶ supports also trigonometric functions (\sin , \cos)
- ▶ available for AMPL and in GAMS and OS
- ▶ Belotti, Lee, Liberti, Margot, and Wächter [2009]



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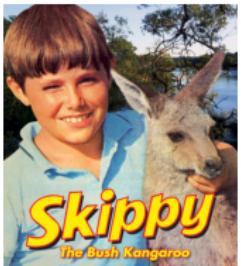
LindoAPI

- ▶ by Y. Lin and L. Schrage (LINDO Systems, Inc.)
- ▶ supports many functions, incl. trigonometric (\sin , \cos)
- ▶ available as commercial solver within LINDO and GAMS
- ▶ Lin and Schrage [2009]



SCIP (Solving Constraint Integer Programs)

- ▶ by Zuse Institute Berlin, TU Darmstadt, ...
- ▶ part of a constraint integer programming framework
- ▶ free for academic use, available for AMPL and in GAMS
- ▶ Berthold, Gleixner, Heinz, and Vigerske [2012], Vigerske [2013]



COCONUT (COntinuous CONstraints – Updating the T>echnology)

- ▶ by A. Neumaier, H. Schichl, E. Monfroy (Vienna), et.al.
- ▶ rigorous calculations via interval arithmetics, thus avoiding floating point roundoff errors
- ▶ still in development, no stable release so far
- ▶ Neumaier [2004], Bliek et al. [2001]



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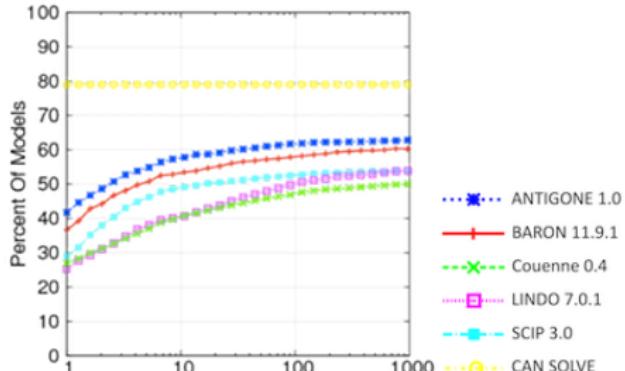


MINOTAUR (Mixed-Integer Nonconvex Optimization Toolbox – Algorithms, Underestimators, Relaxations)

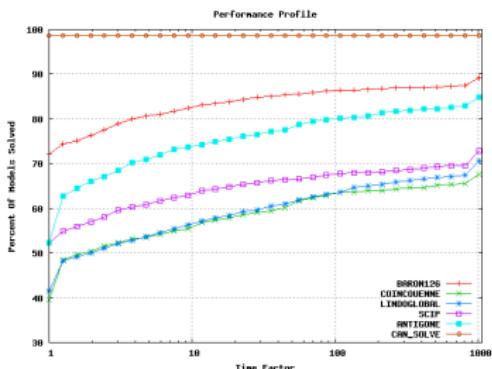
- ▶ by A. Mahajan, S. Leyffer, J. Linderoth, J. Luedtke, T. Munson, et.al. (Argonne, Wisconsin-Madison, IIT Bombay)
- ▶ open source with AMPL interface
- ▶ branch-and-bound with NLP relaxation (or its QP approximation); facilities to handle and manipulate algebraic expression are in place
- ▶ Mahajan and Munson [2010], Mahajan et al. [2012]



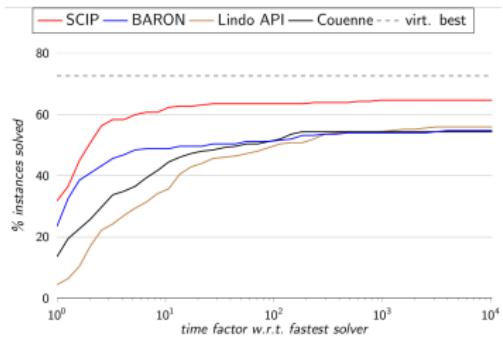
"Best Solver"?



<http://helios.princeton.edu/ANTIGONE/>
1705 instances, NLPs and MINLPs

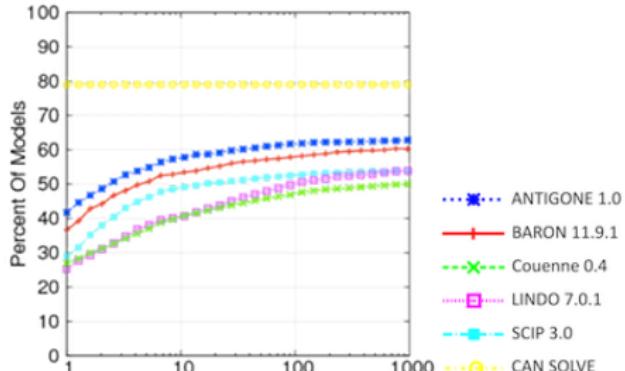


<http://archimedes.cheme.cmu.edu/?q=baron>
1599 instances, NLPs and MINLPs

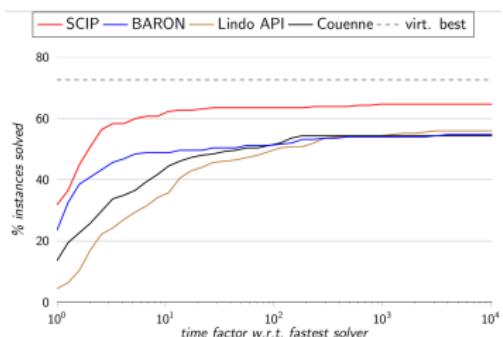


http://www.math.hu-berlin.de/~stefan/SCIP_ISMP12.pdf; 252 instances, MINLPs

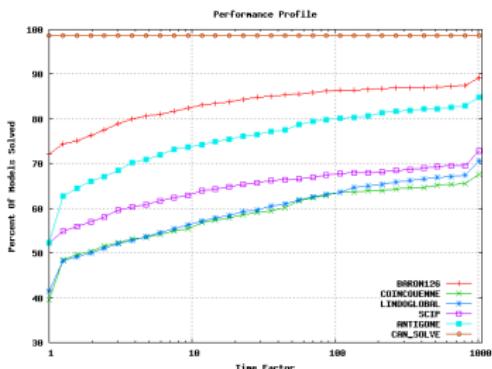
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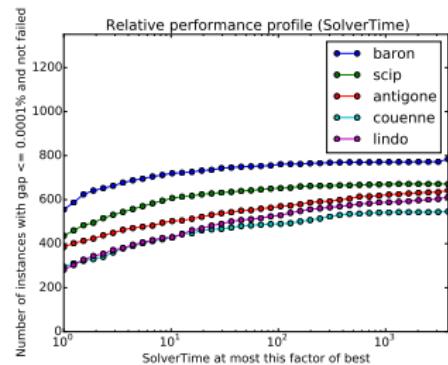
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www.gams.com/presentations/2015_ismp.pdf
≈ 1360 instances, NLPs and MINLPs

Different benchmark sets:

- ▶ So far, there exists no test set that the major solver vendors agree on.
- ▶ Test sets may be unbalanced and contain randomly created instances, trivial or extremely hard instances.

Recall also **Thorsten's talk** “Notes on MIPLIB and Benchmarking”



Where do the differences come from?

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Different performance metrics:

- ▶ When to count an instance as **solved**?
 - ▶ If found a solution and proven optimality: $\text{gap} = 0$?
 - ▶ If found a solution and proven that it is close to optimality: $\text{gap} \leq 10^{-6}$?
 - ▶ If found the best solution among all solvers in the comparison ?
- ▶ Mean solve time, number of solved instances, (extended) (inverted) (filtered) performance profiles, primal/dual/primal-dual integrals, ...
- ▶ Handling of crashes, timeouts, memouts, ...

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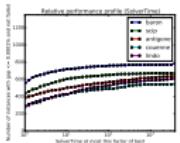
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Numerics:

- ▶ Relative vs. absolute **feasibility tolerances**.
- ▶ Solvers are tuned to their default tolerance.
- ▶ A strictly-feasible ($\text{tolerance} = 0$) solution may exist neither in floating-point nor in rational arithmetics ($\sqrt{2}, \pi, \dots$)
- ▶ In general no simple proofs for **infeasibility or unboundedness**.

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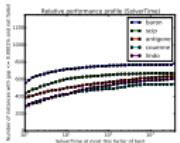




For the performance profile , MINLPLib 2 was used.

However, collecting optimization problems has been popular for a long time, e.g.,

first release	library	problem types
1985	Netlib	Linear Programming
1992	MILPLIB	Mixed-Integer Programming
1993	CUTE	Nonlinear Programming
1998	SDPLib	Semidefinite Programming
1999	CSPLib	Constraint Satisfaction Programming
199x	MacMINLP	Mixed-Integer Nonlinear Programming
2001	GAMS World	LP, MIP, NLP, MINLP, SOCP, MPEC
2003	COCONUT	Nonlinear and Constraint Satisfaction Programming
2008	mintOC	Mixed-Integer Optimal Control
2009	minlp.org	MINLP, General Disjunctive Programming
2011	POLIP	Mixed-Integer Polynomial Programming
2014	CBLIB	Conic Programming
2015	QPLIB (β)	(Mixed-Integer) Quadratic Programming



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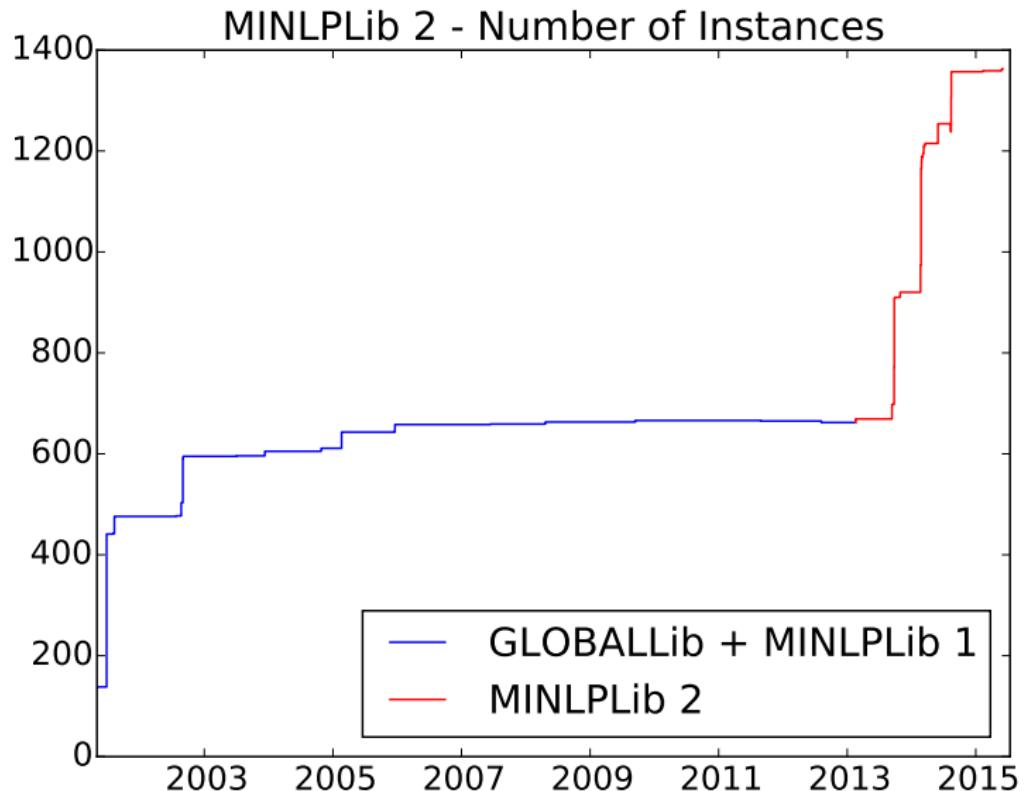
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- ▶ **Initiated in 2001** (as part of GamsWorld/MinIpWorld/GlobalWorld):
M. Bussieck, A. Drud, and A. Meeraus
MINLPLib – A Collection of Test Models for Mixed-Integer Nonlinear Programming
INFORMS Journal on Computing 15, 114–119 (2003)
- ▶ “white-box” NLPs (GLOBALLib) and MINLPs (MINLPLib)
- ▶ instances were **harvested from existing collections**, initially:
 - ▶ GAMS Model Library
 - ▶ MacMINLP (Leyffer)
 - ▶ MINOPT library (Floudas)
 - ▶ Handbook of Test Problems in Local and Global Optimization (Floudas et.al.)
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Since 2013:

- ▶ **Extension and Renovation** (work in progress)
- ▶ Merged GlobalLib and MINPLib 1 into MINLPLib 2.
- ▶ Current version:
<http://www.gamsworld.org/minlp/minplib2/html/index.html>.

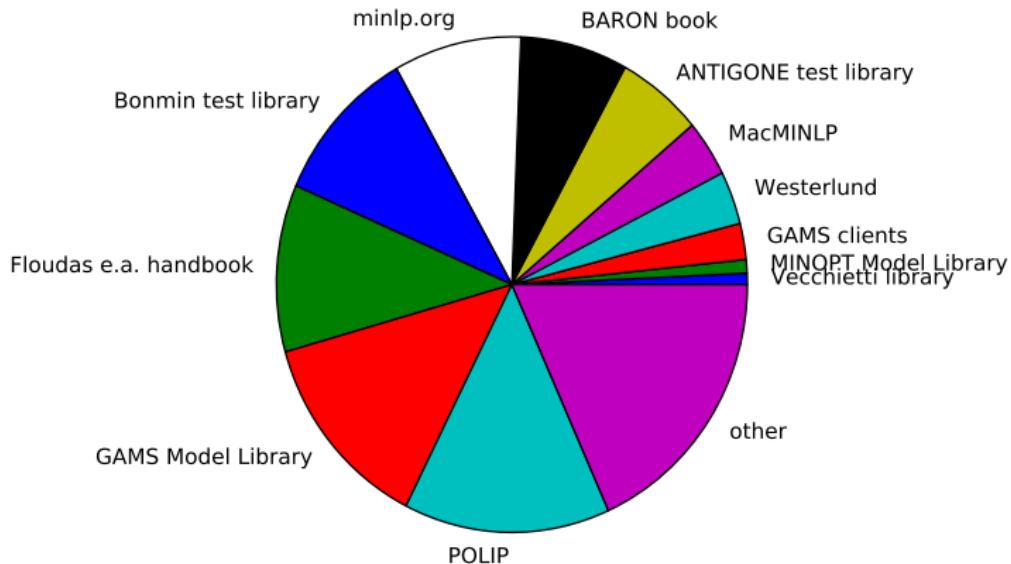


Sources of newly added instances

Harvesting mainly from

- ▶ CMU-IBM open source MINLP project (convex MINLPs)
- ▶ minlp.org
- ▶ POLIP (polynomial MINLPs)

MINLPLib 2 instance sources (1357 in total)



Several formats:

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Query Script:

```
$ ./query.py "(nvars > 4242) & (convex == True)" -c nvars -c ncons
$ ./query.py "(opsin == True) or (opcos == True)"
$ ./query.py "gap > 0.1" -c gap -z open.zip
```

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Quantify Improvements of global MINLP solvers over the last 4 years!

date	GAMS	ANTIGONE	BARON	COUENNE	LINDO	SCIP
08/11	23.7.3	–	9.3.1	0.3	6.1.1.588	–
04/12	23.8.2	–	10.2.0	0.4	7.0.1.421	2.1.1
11/12	23.9.5	–	11.5.2	0.4	7.0.1.497	2.1.2
02/13	24.0.2	–	11.9.1	0.4	7.0.1.497	3.0
07/13	24.1.3	1.1	12.3.3	0.4	8.0.1283.385	3.0
05/14	24.2.3	1.1	12.7.7	0.4	8.0.1694.498	3.0
09/14	24.3.3	1.1	14.0.3	0.4	8.0.1694.550	3.1
06/15	24.4.6	1.1	14.4.0	0.4	9.0.1983.157	3.1
07/15	24.5 α	1.1	15.6.5	0.5	9.0.1983.157	3.2.0

More Detailed Slides: http://www.gams.com/presentations/2015_ismp.pdf

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 - ▶ 60 small investor portfolio optimization instances
 - ▶ ...

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With 15 co-authors and plenty of time, this would be no problem.

MIPLIB 2010

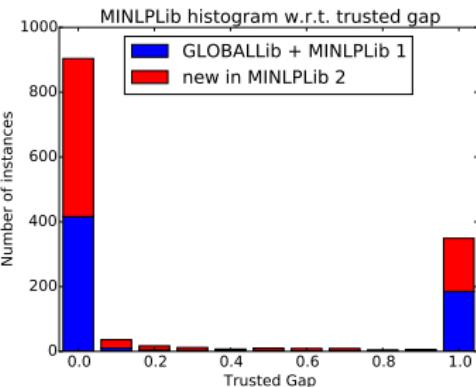
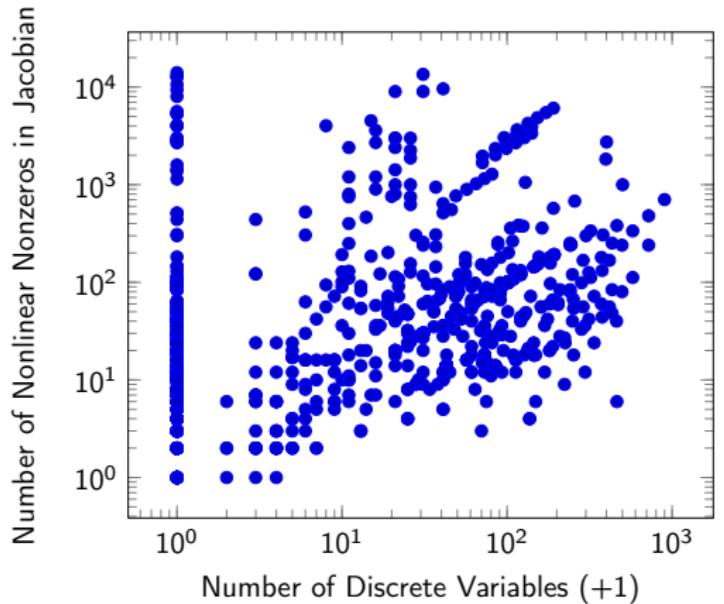
Mixed Integer Programming Library version 5

Thorsten Koch · Tobias Achterberg · Erling Andersen · Oliver Bastert ·
Timo Berthold · Robert E. Bixby · Emilie Danna · Gerald Gamrath ·
Ambros M. Gleixner · Stefan Heinz · Andrea Lodi · Hans Mittelmann ·
Ted Ralphs · Domenico Salvagnin · Daniel E. Steffy · Kati Wolter

But when only 3 weeks left until ISMP: Apply the **P.I.T.T. heuristic**.

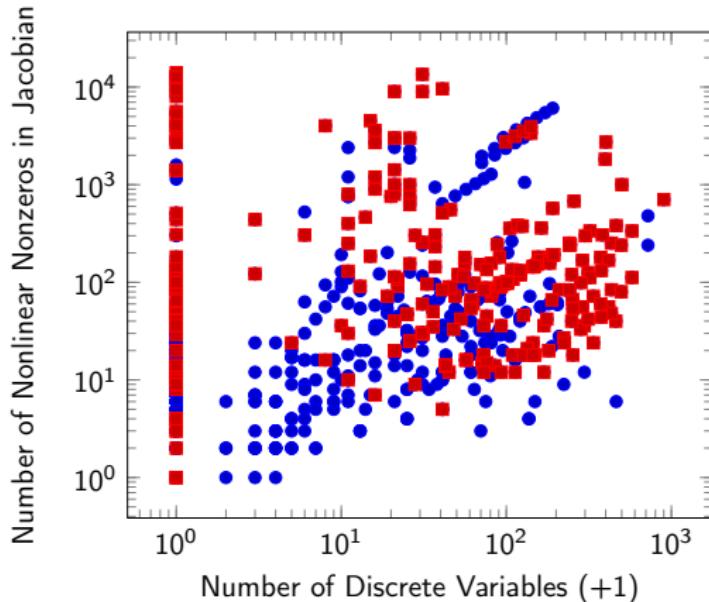
1. Remove intractable instances

- ▶ consider only the 881 instances that are **marked as solved** in MINLPLib 2



2. For each solver separately:

- ▶ Remove instances that are **solved within 60 seconds** by the oldest solver version (e.g., as in GAMS 23.7).
- ▶ Remove instances that the solver **cannot handle** (due to trigonometric functions, SOS, ...).



In case of SCIP:

Prune Instances by Tractability and Triviality Heur.

For SCIP, this leaves 312 instances:

alkylation	clay0304h	ex6_1_1	fo9_ar5_1	house
arki0003	clay0305h	ex6_1_3	gasnet	jbearing25
arki0005	crudeoil_lee2_10	ex6_2_12	genpooling_meyer04	jbearing75
arki0006	crudeoil_lee3_07	ex6_2_14	ghg_1veh	johnall
arki0019	crudeoil_lee3_08	ex6_2_8	ghg_3veh	kall_circles_c6a
arki0024	crudeoil_lee3_09	ex6_2_9	glider100	kall_circles_c6b
autocorr_bern20-10	crudeoil_lee3_10	ex7_2_4	graphpart_2g-0066-0066	kall_circles_c7a
autocorr_bern20-15	crudeoil_li06	ex8_1_7	graphpart_2g-0077-0077	kall_circles_c8a
autocorr_bern25-06	csched1a	ex8_2_1b	graphpart_2g-0088-0088	kall_circlespolygons_c1p
autocorr_bern25-13	edgecross10-060	ex8_2_4b	graphpart_2g-0099-9211	kall_circlespolygons_c1p
autocorr_bern30-04	edgecross10-070	ex8_4_1	graphpart_2pm-0066-0066	kall_circlesrectangles_c1
autocorr_bern35-04	edgecross10-080	ex8_4_3	graphpart_2pm-0077-0777	kall_circlesrectangles_c1
batch0812_nc	edgecross14-039	ex8_4_4	graphpart_2pm-0088-0888	kall_congruentcircles_c1
batchs201210m	edgecross14-058	ex8_4_5	graphpart_2pm-0099-0999	kall_diffcircles_10
bayes2_50	edgecross14-078	ex8_4_8_bnd	graphpart_3g-0334-0334	kall_diffcircles_5b
blend480	edgecross14-176	filter	graphpart_3g-0344-0344	kall_diffcircles_7
blend531	edgecross20-040	fin2bb	graphpart_3g-0444-0444	kall_diffcircles_8
blend718	edgecross22-048	flay05h	graphpart_3pm-0244-0244	kall_diffcircles_9
blend852	emfl050_5_5	fo7	graphpart_3pm-0333-0333	launch
carton7	emfl100_5_5	fo8	graphpart_3pm-0334-0334	lop97icx
casctanks	ethanolh	fo8_ar25_1	graphpart_3pm-0344-0344	mathopt5_7
cecil_13	ethanolm	fo8_ar2_1	graphpart_3pm-0444-0444	mathopt5_8
chem	ex1252a	fo9	graphpart_clique-30	mhw4d
clay0203h	ex14_1_1	fo9_ar25_1	graphpart_clique-40	milinfract
clay0204h	ex14_1_7	fo9_ar2_1	gsg_0001	minlphix
clay0205h	ex4_1_5	fo9_ar3_1	hda	minsurf100
clay0303h	ex4_1_6	fo9_ar4_1	heatech_trigen	...

Prune Instances by Tractability and Triviality Heur.

GAMS

For SCIP, this leaves 312 instances – obvious dominance by some models

alkylation	clay0304h	ex6_1_1	fo9_ar5_1	house
arki0003	clay0305h	ex6_1_3	gasnet	jbearing25
arki0005	crudeoil_lee2_10	ex6_2_12	genpooling_meyer04	jbearing75
arki0006	crudeoil_lee3_07	ex6_2_14	ghg_1veh	johnall
arki0019	crudeoil_lee3_08	ex6_2_8	ghg_3veh	kall_circles_c6a
arki0024	crudeoil_lee3_09	ex6_2_9	glider100	kall_circles_c6b
autocorr_bern20-10	crudeoil_lee3_10	ex7_2_4	graphpart_2g-0066-0066	kall_circles_c7a
autocorr_bern20-15	crudeoil_li06	ex8_1_7	graphpart_2g-0077-0077	kall_circles_c8a
autocorr_bern25-06	csched1a	ex8_2_1b	graphpart_2g-0088-0088	kall_circlespolygons_c1p
autocorr_bern25-13	edgecross10-060	ex8_2_4b	graphpart_2g-0099-9211	kall_circlespolygons_c1p
autocorr_bern30-04	edgecross10-070	ex8_4_1	graphpart_2pm-0066-0066	kall_circlesrectangles_c
autocorr_bern35-04	edgecross10-080	ex8_4_3	graphpart_2pm-0077-0777	kall_circlesrectangles_c
batch0812_nc	edgecross14-039	ex8_4_4	graphpart_2pm-0088-0888	kall_congruentcircles_c
batchs201210m	edgecross14-058	ex8_4_5	graphpart_2pm-0099-0999	kall_diffcircles_10
bayes2_50	edgecross14-078	ex8_4_8_bnd	graphpart_3g-0334-0334	kall_diffcircles_5b
blend480	edgecross14-176	filter	graphpart_3g-0344-0344	kall_diffcircles_7
blend531	edgecross20-040	fin2bb	graphpart_3g-0444-0444	kall_diffcircles_8
blend718	edgecross22-048	flay05h	graphpart_3pm-0244-0244	kall_diffcircles_9
blend852	emfl050_5_5	fo7	graphpart_3pm-0333-0333	launch
carton7	emfl100_5_5	fo8	graphpart_3pm-0334-0334	lop97icx
casctanks	ethanolh	fo8_ar25_1	graphpart_3pm-0344-0344	mathopt5_7
cecil_13	ethanolm	fo8_ar2_1	graphpart_3pm-0444-0444	mathopt5_8
chem	ex1252a	fo9	graphpart_clique-30	mhw4d
clay0203h	ex14_1_1	fo9_ar25_1	graphpart_clique-40	milinfract
clay0204h	ex14_1_7	fo9_ar2_1	gsg_0001	minlphix
clay0205h	ex4_1_5	fo9_ar3_1	hda	minsurf100
clay0303h	ex4_1_6	fo9_ar4_1	heatech_trigen	...

3. Ensure uniqueness of 6-char.-prefix of instances names.

3. Ensure uniqueness of 6-char.-prefix of instances names.

alkylation	clay0304h	ex6_1_1	fe9_ar5_1	house
arki0003	clay0305h	ex6_1_3	gasnet	jbearing25
arki0005	crudeoil_lee2_10	ex6_2_12	genpooling_meyer04	jbearing75
arki0006	crudeoil_lee3_07	ex6_2_14	ghg_1veh	johnall
arki0019	crudeoil_lee3_08	ex6_2_8	ghg_3veh	kall_circles_c6a
arki0024	crudeoil_lee3_09	ex6_2_9	glider100	kall_circles_c6b
autocorr_bern20-10	crudeoil_lee3_10	ex7_2_4	graphpart_2g-0066-0066	kall_circles_c7a
autocorr_bern20-15	crudeoil_li06	ex8_1_7	graphpart_2g-0077-0077	kall_circles_c8a
autocorr_bern25-06	csched1a	ex8_2_1b	graphpart_2g-0088-0088	kall_circlespolygons_c1
autocorr_bern25-13	edgecross10-060	ex8_2_4b	graphpart_2g-0099-9211	kall_circlespolygons_c1
autocorr_bern30-04	edgecross10-070	ex8_4_1	graphpart_2pm-0066-0066	kall_circlesrectangles_c
autocorr_bern35-04	edgecross10-080	ex8_4_3	graphpart_2pm-0077-0777	kall_circlesrectangles_c
batch0812_nc	edgecross14-039	ex8_4_4	graphpart_2pm-0088-0888	kall_congruentcircles_c
batchs201210m	edgecross14-058	ex8_4_5	graphpart_2pm-0099-0999	kall_diffcircles_10
bayes2_50	edgecross14-078	ex8_4_8_bnd	graphpart_3g-0334-0334	kall_diffcircles_5b
blend480	edgecross14-176	filter	graphpart_3g-0344-0344	kall_diffcircles_7
blend531	edgecross20-040	fin2bb	graphpart_3g-0444-0444	kall_diffcircles_8
blend718	edgecross22-048	flay05h	graphpart_3pm-0244-0244	kall_diffcircles_9
blend852	emfl050_5_5	fo7	graphpart_3pm-0333-0333	launch
carton7	emfl100_5_5	fo8	graphpart_3pm-0334-0334	lop97icx
casctanks	ethanolh	fo8_ar25_1	graphpart_3pm-0344-0344	mathopt5_7
cecil_13	ethanolm	fo8_ar2_1	graphpart_3pm-0444-0444	mathopt5_8
chem	ex1252a	fo9	graphpart_clique_30	mhw4d
clay0203h	ex14_1_1	fo9_ar25_1	graphpart_clique_40	milinfract
clay0204h	ex14_1_7	fo9_ar2_1	gsg_0001	minlphix
clay0205h	ex4_1_5	fo9_ar3_1	hda	minsurf100
clay0303h	ex4_1_6	fo9_ar4_1	heatech_trigen	...

In summary:

1. Keep only instances that are marked as **solved** in MINLPLib 2.
2. Keep only instances that take ≥ 60 s with **oldest version** of solver and that can be **handled** by solver.
3. Reduce instances with **similar names**.

For SCIP, this reduces from 1363 to 881 to 123 instances:

alkylation	emfl050_5_5	fo9_ar25_1	milinfract	pinene50	
arki0003	emfl100_5_5	gasnet	minlphix	pointpack08	sssd12-05
autocorr_bern20-10	ethanolh	genpooling_meyer04	minsurf100	pooling_epa1	sssd15-04
batch0812_nc	ex1252a	ghg_1veh	multiplants_mtg1a	prob07	sssd16-07
batchs201210m	ex14_1_1	ghg_3veh	no7_ar3_1	process	sssd18-06
bayes2_50	ex4_1_5	glider100	nous1	procsyn	sssd20-04
blend480	ex6_1_1	graphpart_2g-0066-00609		prolog	sssd25-04
blend531	ex6_2_12	gsg_0001	nvs22	qp3	st_e35
blend718	ex7_2_4	hda	o7	routingdelay_bigm	stockcycle
blend852	ex8_1_7	heatexch_trigen	o7_2	rsyn0805m02h	supplychai
carton7	ex8_2_1b	house	o7_ar25_1	sepasequ_convent	syn10m03h
casctanks	ex8_4_1	jbearing25	o7_ar3_1	sfacloc2_2_80	syn15m02h
cecil_13	filter	johnall	o7_ar4_1	slay07h	syn20m02h
chem	fin2bb	kall_circles_c6a	o7_ar5_1	slay09h	syn30h
clay0203h	flay05h	kall_diffcircles_108_ar4_1		slay10h	syn30m02h
clay0303h	fo7	launch	o9_ar4_1	smallinvDAXr1b020-022	syn40h
crudeoil_lee2_10	fo8	lop97icx	oil	sporttournament14	syn40m02h
csched1a	fo8_ar25_1	mathopt5_7	oil2	squf1010-025	
edgecross10-060	fo9	mhw4d	parallel	sssd08-04	

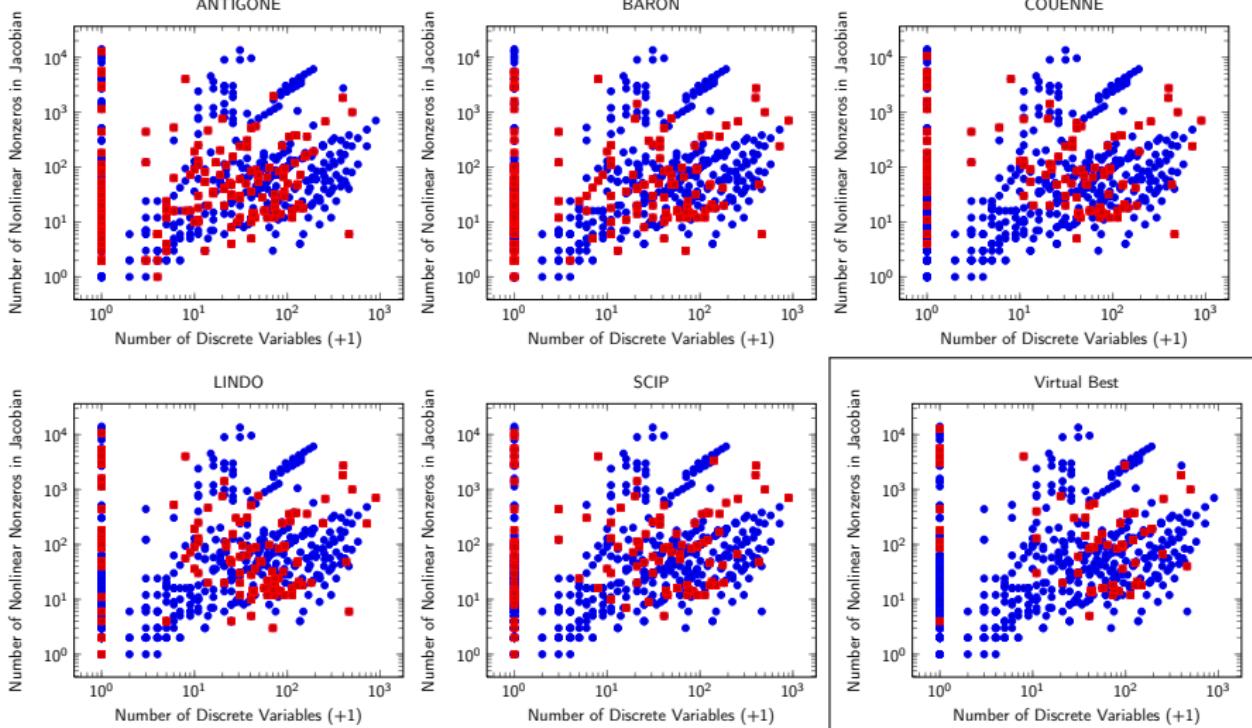
date	GAMS	ANTIGONE	BARON	COUENNE	LINDO	SCIP
08/11	23.7.3	–	9.3.1	0.3	6.1.1.588	–
04/12	23.8.2	–	10.2.0	0.4	7.0.1.421	2.1.1
11/12	23.9.5	–	11.5.2	0.4	7.0.1.497	2.1.2
02/13	24.0.2	–	11.9.1	0.4	7.0.1.497	3.0
07/13	24.1.3	1.1	12.3.3	0.4	8.0.1283.385	3.0
05/14	24.2.3	1.1	12.7.7	0.4	8.0.1694.498	3.0
09/14	24.3.3	1.1	14.0.3	0.4	8.0.1694.550	3.1
06/15	24.4.6	1.1	14.4.0	0.4	9.0.1983.157	3.1
07/15	24.5 α	1.1	15.6.5	0.5	9.0.1983.157	3.2.0

```
for GAMS in $GAMSS ; do
    for SOLVER in $SOLVERS($GAMS) ; do
        for INSTANCE in $TESTSET($SOLVER) ; do
            sbatch --exclusive --time=0:1800 $GAMS $INSTANCE SOLVER=$SOLVER
        done
    done
done
```

Hardware: Dell PowerEdge M1000e, 48GB RAM, Intel Xeon X5672@3.2GHz

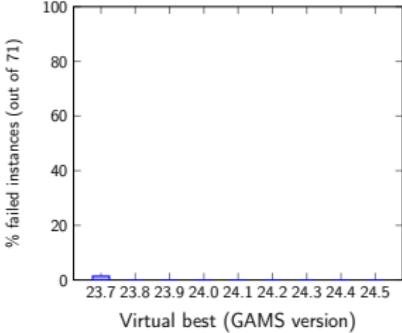
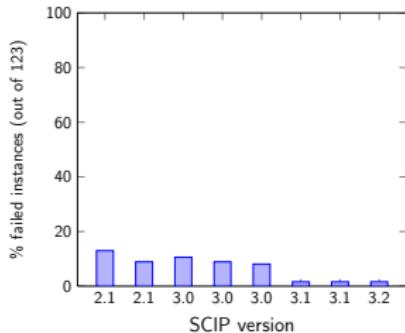
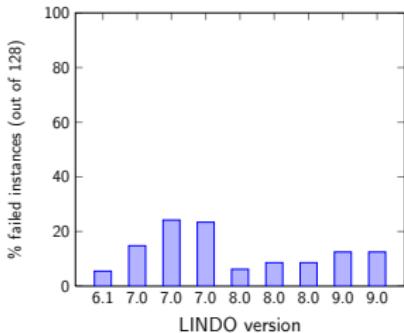
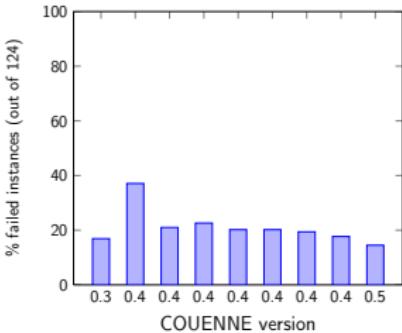
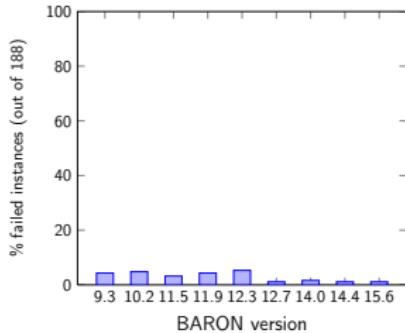
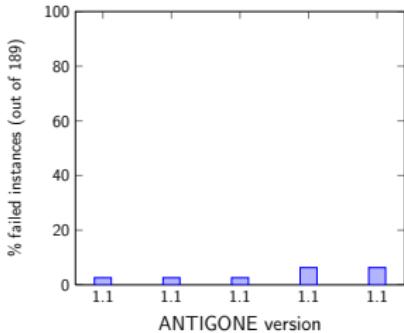
"Virtual Best" Solver

- ▶ common subset of instances (71 many)
- ▶ for each instance and GAMS version, pick **best results among all solvers**

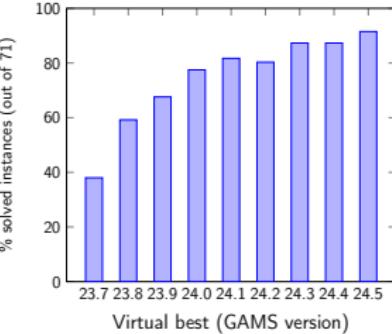
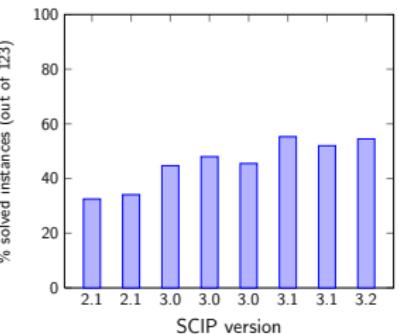
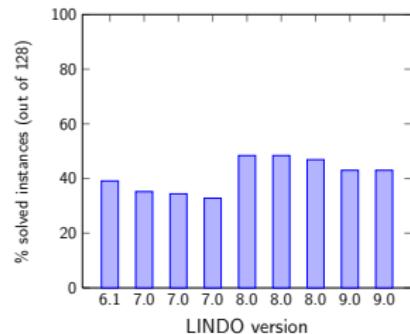
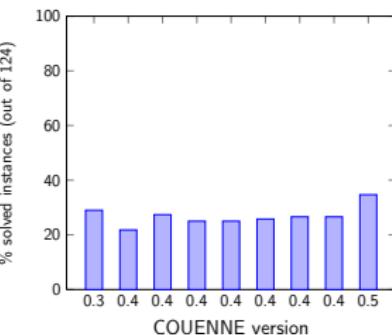
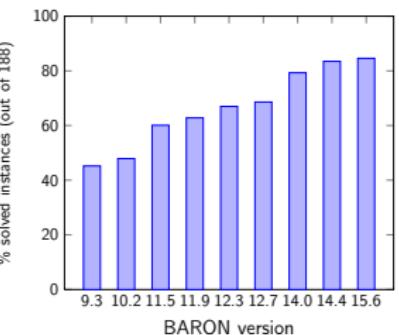
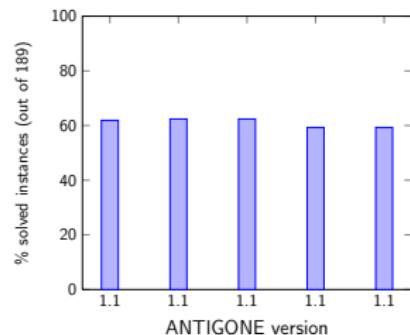


A solver **failed**, if it

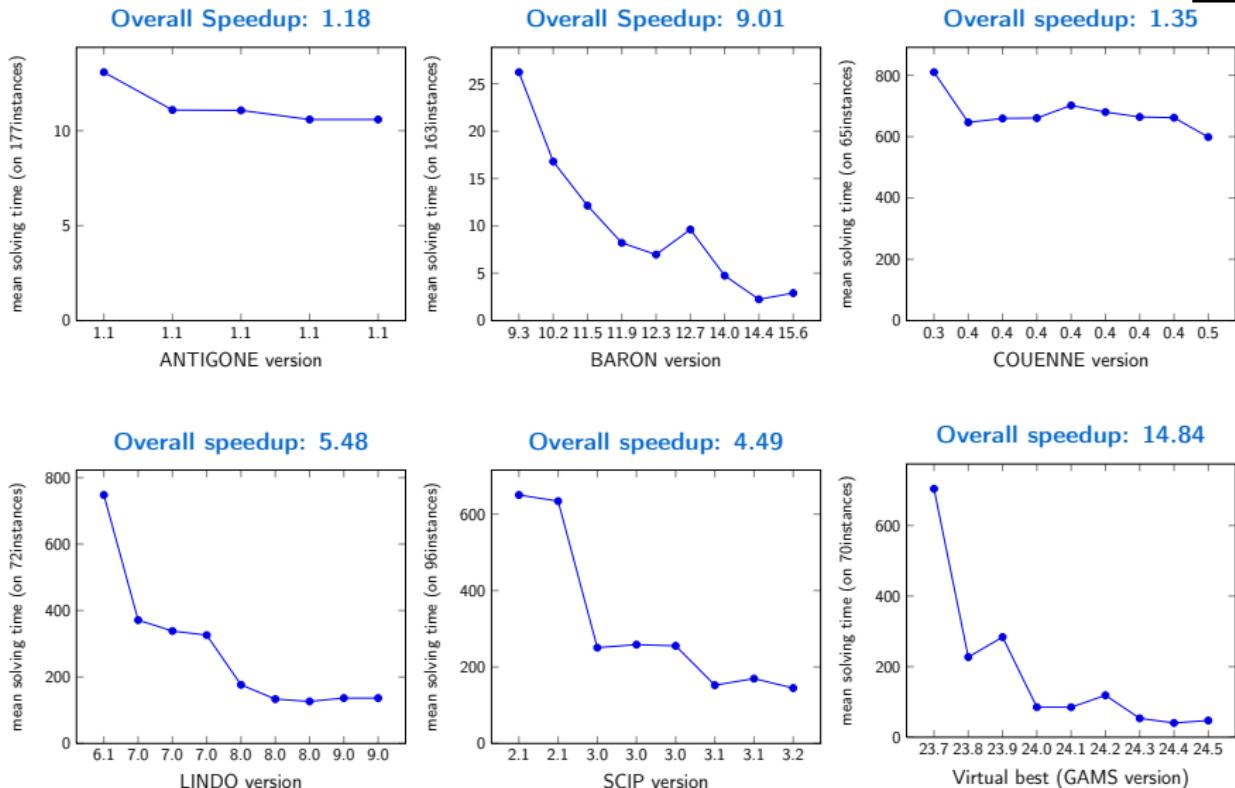
- ▶ crashed, or
- ▶ reported an infeasible point as feasible (tolerance: 10^{-4}), or
- ▶ reported a suboptimal solution as optimal (tolerance: 10^{-4})



Solved: solver did **not fail** and reports a relative optimality **gap** $\leq 10^{-4}$



Mean solve time on instances that never failed



Pietro Belotti, Jon Lee, Leo Liberti, F. Margot, and Andreas Wächter. Branching and bounds tightening techniques for non-convex MINLP. *Optimization Methods and Software*, 24(4-5): 597–634, 2009. doi: 10.1080/10556780903087124.

Timo Berthold, Ambros M. Gleixner, Stefan Heinz, and Stefan Vigerske. Analyzing the computational impact of MIQCP solver components. *Numerical Algebra, Control and Optimization*, 2(4):739–748, 2012. doi: 10.3934/naco.2012.2.739.

Christian Blieck, Peter Spellucci, Luis N. Vicente, Arnold Neumaier, Laurent Granvilliers, Eric Monfroy, Frederic Benhamou, Etienne Huens, Pascal Van Hentenryck, Djamilia Sam-Haroud, and Boi Faltings. Algorithms for solving nonlinear constrained and optimization problems: The state of the art. Technical report, Universität Wien, 2001. URL <http://www.mat.univie.ac.at/~neum/glopt/coconut/StArt.html>.

Youdong Lin and Linus Schrage. The global solver in the LINDO API. *Optimization Methods & Software*, 24(4–5):657–668, 2009. doi: 10.1080/10556780902753221.

Ashutosh Mahajan and Todd Munson. Exploiting second-order cone structure for global optimization. Technical Report ANL/MCS-P1801-1010, Argonne National Laboratory, 2010. URL http://www.optimization-online.org/DB_HTML/2010/10/2780.html.

Ashutosh Mahajan, Sven Leyffer, and Christian Kirches. Solving mixed-integer nonlinear programs by QP-diving. Preprint ANL/MCS-P2071-0312, Argonne National Laboratory, 2012. URL http://www.optimization-online.org/DB_HTML/2012/03/3409.html.

Ruth Misener. Novel Global Optimization Methods: Theoretical and Computational Studies on Pooling Problems with Environmental Constraints. PhD thesis, Princeton University, 2012.
URL <http://arks.princeton.edu/ark:/88435/dsp015q47rn787>.

Ruth Misener and Christodoulos A. Floudas. Global optimization of mixed-integer quadratically-constrained quadratic programs (MIQCQP) through piecewise-linear and edge-concave relaxations. *Mathematical Programming*, 136(1):155–182, 2012a. doi: 10.1007/s10107-012-0555-6.

Ruth Misener and Christodoulos A. Floudas. GloMIQO: Global mixed-integer quadratic optimizer. *Journal of Global Optimization*, 57(1):3–50, 2012b. doi: 10.1007/s10898-012-9874-7.

Ruth Misener and Christodoulos A. Floudas. ANTIGONE: Algorithms for coNTinuous / Integer Global Optimization of Nonlinear Equations. *Journal of Global Optimization*, 59(2-3): 503–526, 2014. doi: 10.1007/s10898-014-0166-2.

Arnold Neumaier. Complete search in continuous global optimization and constraint satisfaction. In *Acta Numerica*, volume 13, chapter 4, pages 271–369. Cambridge University Press, 2004. doi: 10.1017/S0962492904000194.

Mohit Tawarmalani and Nikolaos V. Sahinidis. Convexification and Global Optimization in Continuous and Mixed-Integer Nonlinear Programming: Theory, Algorithms, Software, and Applications, volume 65 of *Nonconvex Optimization and Its Applications*. Kluwer Academic Publishers, 2002. doi: 10.1007/978-1-4757-3532-1.

Mohit Tawarmalani and Nikolaos V. Sahinidis. Global optimization of mixed-integer nonlinear programs: A theoretical and computational study. [Mathematical Programming](#), 99(3): 563–591, 2004. doi: 10.1007/s10107-003-0467-6.

Mohit Tawarmalani and Nikolaos V. Sahinidis. A polyhedral branch-and-cut approach to global optimization. [Mathematical Programming](#), 103(2):225–249, 2005. doi: 10.1007/s10107-005-0581-8.

Stefan Vigerske. [Decomposition in Multistage Stochastic Programming and a Constraint Integer Programming Approach to Mixed-Integer Nonlinear Programming](#). PhD thesis, Humboldt-Universität zu Berlin, 2013. urn:nbn:de:kobv:11-100208240.