

# Introducton to COIN-OR Tools for Optimization

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- 2 Overview of Projects
- 3 Using COIN
  - Optimization Services
  - SYMPHONY
  - CHiPPS
  - DECOMP
- 4 Conclusion

# Brief Bio

- BS and MS in Mathematics from Carnegie Mellon in 1991
- PhD. in Operations Research from Cornell in 1995
- Currently
  - Associate professor at Lehigh University
  - Director of the Laboratory for Computation Optimization Research at Lehigh (COR@L).
  - Chair of the Technical Leadership Council of the COIN-OR Foundation.
- Research interests
  - Computational optimization
  - Discrete/Combinatorial optimization theory
  - Parallel/Grid computing
  - Software development

# Brief History of COIN-OR

- The **Common Optimization Interface for Operations Research Initiative** was an initiative launched by IBM at ISMP in 2000.
- IBM seeded an open source repository with four initial projects and created a Web site.
- The goal was to develop the project and then hand it over to the community.
- The project has now grown to be self-sustaining and was spun off as a nonprofit educational foundation in the U.S. several years ago.
- The name was also changed to the **Computational Infrastructure for Operations Research** to reflect a broader mission.

# What is COIN-OR Today?

## The COIN-OR Foundation

- A **non-profit foundation** promoting the development and use of interoperable, open-source software for operations research.
- A **consortium** of researchers in both industry and academia dedicated to improving the state of computational research in OR.
- A **venue** for developing and maintaining standards.
- A **forum** for discussion and interaction between practitioners and researchers.

## The COIN-OR Repository

- A **collection** of interoperable software tools for building optimization codes, as well as a few stand alone packages.
- A **venue for peer review** of OR software tools.
- A **development platform** for open source projects, including an SVN repository,

# The COIN-OR Foundation

- The foundation has been up and running for several years.
- We have two boards.
  - A **strategic board** to set overall direction
  - A **technical board** to advise on technical issues
- The boards are composed of members from both industry and academia, as well as balanced across disciplines.
- Membership in the foundation is available to both individuals and institutions.
- The foundation Web site and repository are hosted by **INFORMS**.

# What You Can Do With COIN

- We currently have 30+ projects and more are being added all the time.
- Most projects are now licensed under the [EPL](#) (very permissive).
- COIN has solvers for most common optimization problem classes.
  - Linear programming
  - Nonlinear programming
  - Mixed integer linear programming
  - Mixed integer nonlinear programming (convex and nonconvex)
  - Stochastic linear programming
  - Semidefinite programming
  - Graph problems
  - Combinatorial problems (VRP, TSP, SPP, etc.)
- COIN has various utilities for reading/building/manipulating/preprocessing optimization models and getting them into solvers.
- COIN has overarching frameworks that support implementation of broad algorithm classes.
  - Parallel search
  - Branch and cut (and price)
  - Decomposition-based algorithms

# COIN-OR Projects Overview: Linear Optimization)

- **Clp**: COIN LP Solver  
Project Manager: John Forrest
- **Cbc**: COIN Branch and Cut  
Project Manager: John Forrest
- **SYMPHONY**: a flexible integer programming package that supports shared and distributed memory parallel processing, biobjective optimization, warm starting, sensitivity analysis, application development, etc.  
Project Manager: Ted Ralphs
- **BLIS**: Parallel IP solver built to test the scalability of the CHiPPS framework.  
Project Manager: Ted Ralphs

# COIN-OR Projects Overview: Nonlinear Optimization

- **Ipopt:** Interior Point OPTimizer implements interior point methods for solving nonlinear optimization problems.

Project Manager: Andreas Wächter

- **Bonmin:** Basic Open-source Nonlinear Mixed INteger programming is for (convex) nonlinear integer programming.

Project Manager: Pierre Bonami

- **Couenne:** Solver for nonconvex nonlinear integer programming problems.

Project Manager: Pietro Belloti

# COIN-OR Projects Overview: Modeling and Interfaces

- **Osi**: Open solver interface is a generic API for linear and mixed integer linear programs.  
**Project Manager**: Matthew Saltzman
- **GAMSLinks**: Allows you to use the GAMS algebraic modeling language and call COIN-OR solvers.  
**Project Manager**: Stefan Vigerske
- **FLOPC++**: An open-source modeling system.  
**Project Manager**: Tim Hultberg
- **CoinMP**: A callable library that wraps around CLP and CBC, providing an API similar to CPLEX, XPRESS, Gurobi, etc.  
**Project Manager**: Bjarni Kristjansson
- **Optimization Services**: A framework defining data interchange formats and providing tools for calling solvers locally and remotely through Web services.  
**Project Managers**: Jun Ma, Gus Gassmann, and Kipp Martin

# COIN-OR Projects Overview: Frameworks

- **Bcp**: A generic framework for implementing branch, cut, and price algorithms.  
**Project Manager**: Laci Ladanyi
- **CHiPPS**: A framework for developing parallel tree search algorithms.  
**Project Manager**: Ted Ralphs
- **DECOMP (coming very soon)**: A framework for implementing decomposition-based algorithms for integer programming, including Dantzig-Wolfe, Lagrangian relaxation, cutting plane, and combinations.  
**Project Manager**: Ted Ralphs

# COIN-OR Projects Overview: Miscellaneous)

- **CppAD**: a package for doing algorithmic differentiation, a key ingredient in modern nonlinear optimization codes.

**Project Manager**: Brad Bell

- **CSDP**: A solver for semi-definite programs

**Project Manager**: Brian Borchers

- **DFO**: An algorithm for derivative free optimization.

**Project Manager**: Katya Scheinburg

# CoinAll, CoinBinary, BuildTools, and TestTools

- Many of the tools mentioned interoperate by using the configuration and build utilities provided by the **BuildTools** project.
- The **BuildTools** includes autoconf macros and scripts that allow PMs to smoothly integrate code from other projects into their own.
- The **CoinAll** project is an über-project that includes a set of mutually interoperable projects and specifies specific sets of versions that are compatible.
- The **TestTools** project is the focal point for testing of COIN code.
- The **CoinBinary** project is a long-term effort to provide pre-built binaries for popular platforms.
  - Installers for Windows
  - RPMs for Linux
  - .debs for Linux
- You can download **CoinAll** (source and/or binaries) here: here:

<http://projects.coin-or.org/svn/CoinBinary/CoinAll/>

<http://www.coin-or.org/download/binary/CoinAll>

# Building CoinAll

- For MSVC++, there are project files provided.
- In \*nix environments (Linux, Solaris, AIX, CYGWIN, MSys, etc.)

## Installing CoinAll

```
svn co http://projects.coin-or.org/svn/CoinBinary/CoinAll/releases/1.3.0 \  
    CoinAll-1.3.0  
cd CoinAll-1.3.0  
./get.AllThirdParty  
mkdir build  
cd build  
../configure --enable-gnu-packages -C [--prefix=/path/to/install/location]  
make -j 2  
make test  
make install
```

# Optimization Services (OS)

Optimization Services (OS) integrates numerous COIN-OR projects. The OS project provides:

- A set of **XML based standards** for representing optimization instances (**OSiL**), optimization results (**OSrL**), and optimization solver options (**OSoL**).
- A **uniform API** for constructing optimization problems (linear, nonlinear, discrete) and passing them to solvers.
- A command line executable **OSSolverService** for reading problem instances in several formats and calling a solver either locally or remotely.
- Utilities that convert AMPL nl and MPS files into the OSiL format.
- Client side software for creating **Web Services** SOAP packages with OSiL instances and contact a server for solution.
- Standards that facilitate the communication between clients and solvers using Web Services.
- **Server software** that works with Apache Tomcat.

# Solving a Problem on the Command Line

- The OS project provides an single executable `OSSolverService` that can be used to call most COIN solvers.
- To solve a problem in MPS format

```
OSSolverService -mps ../../data/mpsFiles/parinc.mps
```

- The solver also accepts AMPL nl and OSiL formats.
- You can display the results in raw XML, but it's better to print to a file to be parsed.

```
OSSolverService -osil ../../data/osilFiles/parincLinear.osil  
-osrl result.xml
```

- You can then in a browser using XSLT.
  - Copy the stylesheets to your output directory.
  - Open in your browser

# Specifying a Solver

```
OSSolverService -osil ../../data/osilFiles/p0033.osil  
-solver cbc
```

To solve a **linear program** set the solver options to:

- `clp`
- `dylp`

To solve a **mixed-integer linear program** set the solver options to:

- `cbc`
- `symphony`

To solve a **continuous nonlinear program** set the solver options to:

- `ipopt`

To solve a **mixed-integer nonlinear program** set the solver options to:

- `bonmin`
- `couenne`

# Getting a Model into the Solver

- What is the point of the OSiL format?
  - Provides a single interchange standard for all classes of mathematical programs.
  - Makes it easy to use existing tools for defining Web services, etc.
  - Generally, however, one would not build an OSiL file directly.
- To construct a model and pass it to a COIN solver, there are several routes.
  - Use a modeling language—AMPL, GAMS, and MPL work with COIN-OR solvers.
  - Use FlopC++.
  - Build the instance in memory using COIN-OR utilities.

# Using AMPL with OS

To use OS to call solvers in AMPL, you specify the `OSAmplClient` as the solver.

```
model hs71.mod;
# tell AMPL that the solver is OSAmplClient
option solver OSAmplClient;

# now tell OSAmplClient to use Ipopt
option OSAmplClient_options "solver ipopt";

# now solve the problem
solve;
```

In order to call a remote solver service, set the solver `service` option to the address of the remote solver service.

```
option ipopt_options
"service http://gsbkip.chicagogsb.edu/os/OSSolverService.jws";
```

# Building a Model in Memory using OS

**Step 1:** Construct an instance in a solver-independent format using the OS API.

**Step 2:** Create a solver object

```
CoinSolver *solver = new CoinSolver();  
solver->sSolverName = "clp";
```

**Step 3:** Feed the solver object the instance created in Step 1.

```
solver->osinstance = osinstance;
```

**Step 4:** Build solver-specific model instance

```
solver->buildSolverInstance();
```

**Step 5:** Solve the problem.

```
solver->solve();
```

# Building an OS Instance

The `OSInstance` class provides an API for constructing models and getting those models into solvers.

- `set()` and `add()` methods for creating models.
- `get()` methods for getting information about a problem.
- `calculate()` methods for finding gradient and Hessians using algorithmic differentiation.

# Building an OS Instance (cont.)

- Create an `OSInstance` object.

```
OSInstance *osinstance = new OSInstance();
```

- Put some variables in

```
osinstance->setVariableNumber( 2);  
osinstance->addVariable(0, "x0", 0, OSDBL_MAX, 'C', OSNAN, "");  
osinstance->addVariable(1, "x1", 0, OSDBL_MAX, 'C', OSNAN, "");
```

- There are methods for constructing
  - the objective function
  - constraints with all linear terms
  - quadratic constraints
  - constraints with general nonlinear terms

# Other Options for Linear Problems

- `CoinUtils` has a number of utilities for constructing instances.
  - `PackedMatrix` and `PackedVector` classes.
  - `CoinBuild`
  - `CoinModel`
- `Osi` provides an interface for building models and getting them into solvers for linear probes.

# Quick Summary of SYMPHONY Features

## Using SYMPHONY

- C Library API
- OSI C++ interface
- Interactive shell
- AMPL/GMPL, GAMS, FLOPC++
- Framework for customization

## Advanced Features

- Shared and distributed memory parallel MIP (since 1994)
- Biobjective MIP
- Warm starting for MIP
- Sensitivity analysis for MIP

## SYMPHONY Applications

- TSP/VRP
- Set Partitioning Problem
- Mixed Postman Problem
- Capacitated Node Routing
- Multicriteria Knapsack

# Quick Introduction to CHiPPS

- CHiPPS stands for COIN-OR High Performance Parallel Search.
- CHiPPS is a set of C++ class libraries for implementing **tree search** algorithms for both sequential and parallel environments.

## CHiPPS Components (Current)

### ALPS (Abstract Library for Parallel Search)

- is the search-handling layer (parallel and sequential).
- provides various search strategies based on node priorities.

### BiCePS (Branch, Constrain, and Price Software)

- is the data-handling layer for relaxation-based optimization.
- adds notion of **variables** and **constraints**.
- assumes iterative bounding process.

### BLIS (BiCePS Linear Integer Solver)

- is a concretization of BiCePS.
- specific to models with **linear** constraints and objective function.

# ALPS: Design Goals

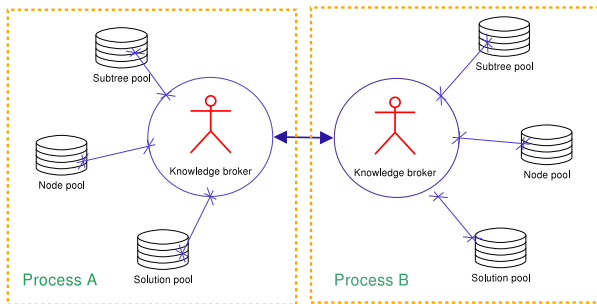
- Intuitive object-oriented class structure.
  - `AlpsModel`
  - `AlpsTreeNode`
  - `AlpsNodeDesc`
  - `AlpsSolution`
  - `AlpsParameterSet`
- Minimal algorithmic assumptions in the base class.
  - Support for a wide range of problem classes and algorithms.
  - Support for constraint programming.
- Easy for user to develop a custom solver.
- Design for *parallel scalability*, but operate effective in a sequential environment.
- Explicit support for *memory compression* techniques (packing/differencing) important for implementing optimization algorithms.

# ALPS: Overview of Features

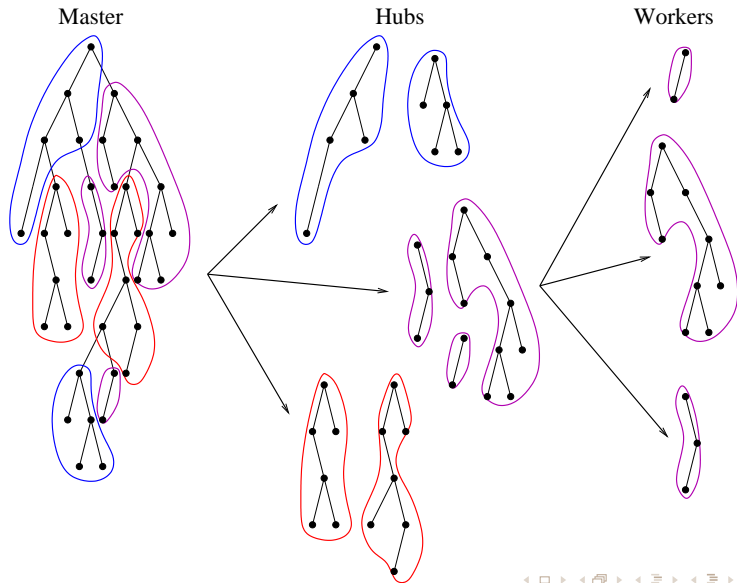
- The design is based on a very general concept of *knowledge*.
- Knowledge is shared *asynchronously* through *pools* and *brokers*.
- Management overhead is reduced with the *master-hub-worker* paradigm.
- Overhead is decreased using *dynamic task granularity*.
- Two *static load balancing* techniques are used.
- Three *dynamic load balancing* techniques are employed.
- Uses *asynchronous* messaging to the highest extent possible.
- A scheduler on each process manages tasks like
  - node processing,
  - load balancing,
  - update search states, and
  - termination checking, etc.

# Knowledge Sharing

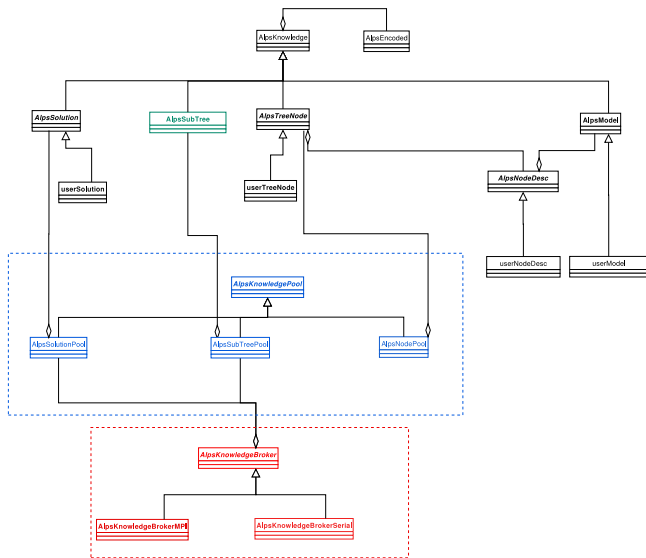
- All knowledge to be shared is derived from a single base class and has an associated *encoded form*.
- Encoded form is used for **identification**, **storage**, and **communication**.
- Knowledge is maintained by one or more *knowledge pools*.
- The knowledge pools communicate through *knowledge brokers*.



# Master-Hub-Worker Paradigm



# Alps Class Hierarchy



# Using ALPS: A Knapsack Solver

The formulation of the binary knapsack problem is

$$\max \left\{ \sum_{i=1}^m p_i x_i : \sum_{i=1}^m s_i x_i \leq c, x_i \in \{0, 1\}, i = 1, 2, \dots, m \right\}, \quad (1)$$

We derive the following classes:

- `KnapModel` (from `AlpsModel`): Stores the data used to describe the knapsack problem and implements `readInstance()`
- `KnapTreeNode` (from `AlpsTreeNode`): Implements `process()` (bound) and `branch()`
- `KnapNodeDesc` (from `AlpsNodeDesc`): Stores information about which variables/items have been fixed by branching and which are still free.
- `KnapSolution` (from `AlpsSolution`) Stores a solution (which items are in the knapsack).

# Using ALPS: A Knapsack Solver

Then, supply the main function.

```
int main(int argc, char* argv[])
{
    KnapModel model;

    #if defined(SERIAL)
        AlpsKnowledgeBrokerSerial broker(argc, argv, model);
    #elif defined(PARALLEL_MPI)
        AlpsKnowledgeBrokerMPI broker(argc, argv, model);
    #endif

    broker.search();
    broker.printResult();
    return 0;
}
```

# BiCePS: Support for Relaxation-based Optimization

- Adds notion of *modeling objects* (variables and constraints).
- Models are built from sets of such objects.
- Bounding is an iterative process that produces new objects.
- A differencing scheme is used to store the difference between the descriptions of a child node and its parent.

```
struct BcpsObjectListMod
{
    int    numRemove;
    int*   posRemove;
    int    numAdd;
    BcpsObject **objects;
    BcpsFieldListMod<double> lbHard;
    BcpsFieldListMod<double> ubHard;
    BcpsFieldListMod<double> lbSoft;
    BcpsFieldListMod<double> ubSoft;
};
```

```
template<class T>
struct BcpsFieldListMod
{
    bool relative;
    int  numModify;
    int  *posModify;
    T    *entries;
};
```

## MILP

$$\min \quad c^T x \quad (2)$$

$$s.t. \quad Ax \leq b \quad (3)$$

$$x_i \in \mathbb{Z} \quad \forall i \in I \quad (4)$$

where  $(A, b) \in \mathbb{R}^{m \times (n+1)}$ ,  $c \in \mathbb{R}^n$ .

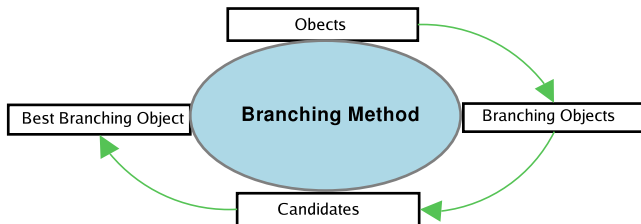
## Basic Algorithmic Components

- Bounding method.
- Branching scheme.
- Object generators.
- Heuristics.

# BLIS: Branching Scheme

BLIS Branching scheme comprise three components:

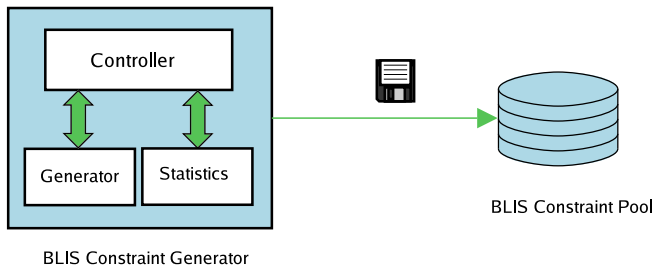
- **Object:** has feasible region and can be branched on.
- **Branching Object:**
  - is created from objects that do not lie in they feasible regions or objects that will be beneficial to the search if branching on them.
  - contains instructions for how to conduct branching.
- **Branching method:**
  - specifies how to create a set of candidate branching objects.
  - has the method to compare objects and choose the best one.



# BLIS: Constraint Generators

BLIS constraint generator:

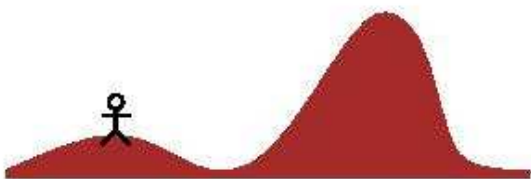
- provides an interface between BLIS and the algorithms in COIN/Cgl.
- provides a base class for deriving specific generators.
- has the ability to specify rules to control generator:
  - where to call: root, leaf?
  - how many to generate?
  - when to activate or disable?
- contains the statistics to guide generating.



# BLIS: Heuristics

BLIS primal heuristic:

- defines the functionality to search for solutions.
- has the ability to specify rules to control heuristics.
  - where to call: before root, after bounding, at solution?
  - how often to call?
  - when to activate or disable?
- collects statistics to guide the heuristic.
- provides a base class for deriving specific heuristics.



# BLIS Applications

BLIS can be customized easily by deriving the base C++ classes.

## Sample Applications (Scott DeNegre, Ted Ralphs, Yan Xu, and others)

- Vehicle Routing Problem (VRP)
- Traveling Salesman Problem (TSP)
- Mixed Integer Bilevel Programming (MiBS)

# BLIS Applications: VRP Formulation

$$\min \sum_{e \in E} c_e x_e$$

$$\sum_{e=\{0,j\} \in E} x_e = 2k, \quad (5)$$

$$\sum_{e=\{i,j\} \in E} x_e = 2 \quad \forall i \in N, \quad (6)$$

$$\sum_{\substack{e=\{i,j\} \in E \\ i \in S, j \notin S}} x_e \geq 2b(S) \quad \forall S \subset N, |S| > 1, \quad (7)$$

$$0 \leq x_e \leq 1 \quad \forall e = \{i,j\} \in E, i,j \neq 0, \quad (8)$$

$$0 \leq x_e \leq 2 \quad \forall e = \{i,j\} \in E, \quad (9)$$

$$x_e \in \mathbb{Z} \quad \forall e \in E. \quad (10)$$

# BLIS Applications: VRP

First, derive a few subclasses to specify the algorithm and model

- `VrpModel` (from `BlisModel`),
- `VrpSolution` (from `BlisSolution`),
- `VrpCutGenerator` (from `BlisConGenerator`),
- `VrpHeurTSP` (from `BlisHeuristic`),
- `VrpVariable` (from `BlisVariable`), and
- `VrpParameterSet` (from `AlpsParameterSet`).

# BLIS Applications: VRP (cont.)

```
int main(int argc, char* argv[])
{
    OsiClpSolverInterface lpSolver;
    VrpModel model;
    model.setSolver(&lpSolver);
#ifdef COIN_HAS_MPI
    AlpsKnowledgeBrokerMPI broker(argc, argv, model);
#else
    AlpsKnowledgeBrokerSerial broker(argc, argv, model);
#endif
    broker.search(&model);
    broker.printBestSolution();
    return 0;
}
```

## Shameless Self-Promotion

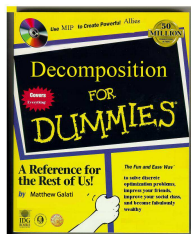
In October, 2007, the VRP/TSP solver won the Open Contest of Parallel Programming at the 19th International Symposium on Computer Architecture and High Performance Computing.

# DECOMP Framework: Motivation

## DECOMP Framework

**DECOMP** is a software framework that provides a virtual sandbox for testing and comparing various decomposition-based bounding methods.

- It's difficult to compare variants of decomposition-based algorithms.
- The method for separation/optimization over  $\mathcal{P}'$  is the primary custom component of any of these algorithms.
- **DECOMP** abstracts the common, generic elements of these methods.
  - **Key:** The user defines methods in the space of the compact formulation.
  - The framework takes care of reformulation and implementation for all variants.

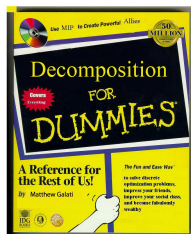


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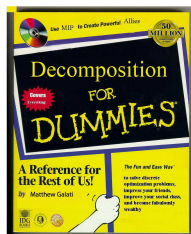


# DECOMP Framework: Motivation

## DECOMP Framework

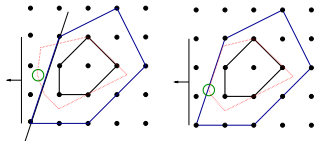
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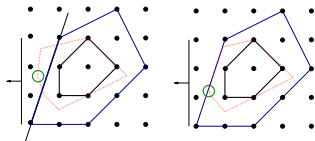
# Traditional Decomposition Methods

The **Cutting Plane Method (CP)** iteratively builds an *outer* approximation of  $\mathcal{P}'$  by solving a **cutting plane generation subproblem**.

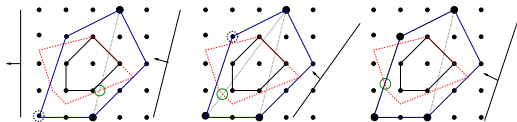


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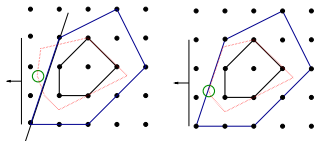


The **Dantzig-Wolfe Method (DW)** iteratively builds an *inner* approximation of  $\mathcal{P}'$  by solving a **column generation subproblem**.

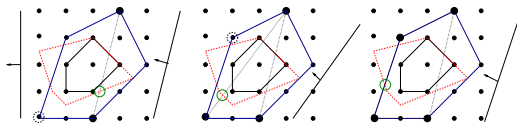


# Traditional Decomposition Methods

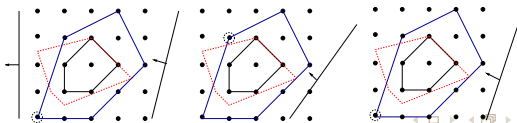
The **Cutting Plane Method (CP)** iteratively builds an *outer* approximation of  $\mathcal{P}'$  by solving a **cutting plane generation subproblem**.



The **Dantzig-Wolfe Method (DW)** iteratively builds an *inner* approximation of  $\mathcal{P}'$  by solving a **column generation subproblem**.



The **Lagrangian Method (LD)** iteratively solves a **Lagrangian relaxation subproblem**.



# Common Threads

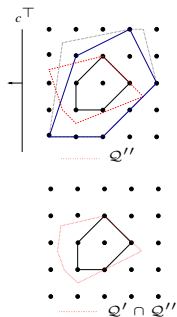
- The **LP bound** is obtained by optimizing over the intersection of two explicitly defined polyhedra.

$$z_{LP} = \min_{x \in \mathbb{R}^n} \{c^T x \mid x \in Q' \cap Q''\}$$

- The **decomposition bound** is obtained by optimizing over the intersection of one explicitly defined polyhedron and one implicitly defined polyhedron.

$$z_{CP} = z_{DW} = z_{LD} = z_D = \min_{x \in \mathbb{R}^n} \{c^T x \mid x \in P' \cap Q''\} \geq z_{LP}$$

- Traditional decomposition-based bounding methods contain two primary steps
  - **Master Problem:** Update the primal/dual solution information.
  - **Subproblem:** Update the approximation of  $P'$ :  $SEP(x, P')$  or  $OPT(c, P')$ .
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# Common Threads

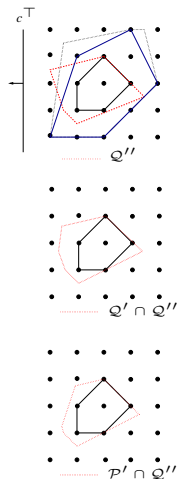
- The **LP bound** is obtained by optimizing over the intersection of two explicitly defined polyhedra.

$$z_{LP} = \min_{x \in \mathbb{R}^n} \{c^T x \mid x \in Q' \cap Q''\}$$

- The **decomposition bound** is obtained by optimizing over the intersection of one explicitly defined polyhedron and one implicitly defined polyhedron.

$$z_{CP} = z_{DW} = z_{LD} = z_D = \min_{x \in \mathbb{R}^n} \{c^T x \mid x \in P' \cap Q''\} \geq z_{LP}$$

- Traditional decomposition-based bounding methods contain two primary steps
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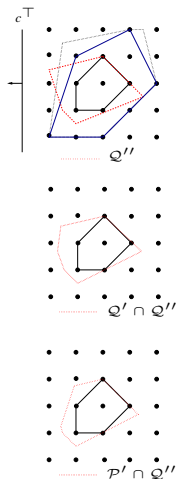
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# DECOMP Framework

- The **DECOMP** framework, written in C++, is accessed through two user interfaces:
  - **Applications Interface**: `DecompApp`
  - **Algorithms Interface**: `DecompAlgo`
- **DECOMP** provides the bounding method for branch and bound.
- **ALPS** (Abstract Library for Parallel Search) provides the framework for parallel tree search.
  - `AlpsDecompModel : public AlpsModel`
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## COIN needs your help!

- Contribute a project
- Help develop an existing project
- Use projects and report bugs
- Volunteer to review new projects
- Develop documentation
- Develop Web site
- Chair a committee

# Questions? & Thank You!